## On a possible logarithmic connection between $|_{fine\ structure\ constant}\ \alpha_0 \cong 137^{-1}$ for example, which is the value Einstein's constant and the fine-structure constant, in relation to a zero-energy **hypothesis**

#### **Abstract**

This paper brings into attention a possible logarithmic connection between Einstein's constant and the fine-structure constant, based on a hypothetical electro-gravitational resistivity of vacuum: we also propose a zero-energy hypothesis (**ZEH**) which is essentially a conservation principle applied on zero-energy that mainly states a general quadratic equation having a pair of conjugate mass solutions for each set of coefficients, thus predicting a new type of mass "symmetry" called here "mass conjugation" between elementary particles (EPs) which predicts the zero/nonzero rest masses of all known/unknown EPs to be conjugated in boson-fermion pairs; ZEH proposes a general formula for all the rest masses of all EPs from Standard model, also indicating a possible bijective connection between the three types of neutrinos and the massless bosons (photon, gluon and the hypothetical graviton), between the electron/positron and the W boson and predicting two distinct types of neutral massless fermions (modelled as conjugates of the Higgs boson and Z boson respectively) which are plausible candidates for dark energy and dark matter. ZEH also offers a new interpretation of Planck length as the approximate length threshold above which the rest masses of all known elementary particles have real number values (with mass units) instead of complex/imaginary number values (as predicted by the unique quadratic equation proposed by ZEH).

**Keywords**: Einstein's constant, fine-structure constant, electrogravitational resistivity of vacuum (EGRV), zero-energy hypothesis (**ZEH**), conservation principle applied on zero-energy, elementary particles (EPs), mass conjugation, neutral massless fermions, dark energy, dark matter, a new interpretation of Planck length;

## I. On a possible logarithmic connection between Einstein's constant and the fine-structure constant

### 1. Introduction

This paper continues the work from other two past articles published by the author [1,2] by arguing for a possible base-2 logarithmic connection between large (gravitational) and small (electromagnetic) dimensionless constants of nature, which can be regarded as an alternative to the notorious Dirac's large number hypothesis.

## 2. Motivating points

If the very large dimensionless physical constants (**DPCs**) (which are gravity-related in general, like the inverse of the gravitational example coupling constant  $\alpha_G^{-1} = \hbar c / (Gm_e^2) \cong 10^{45}$ ) are deeply related with the small DPCs (usually close to 1 and related to quantum mechanics, like the

at rest of the running coupling constant of the electromagnetic field), by any (yet unknown) mathematical function, then a logarithmic function (LF) would be the simplest (and thus the most natural) candidate solution of connecting these large and small DPCs, as other authors also considered in the past [3,4]. Furthermore, even if it is not the case of such a logarithmical connection, possible LFs (connecting those DPCs) would still have to be ruled out first.

#### 3. Observations

#### 3.1 First observation

which, in turn, is always associated with non-zero spacetime curvature (gravity) as implied by General relativity. Furthermore, because the electron (with elementary electromagnetic charge -|e|, rest mass  $m_n$  and rest energy  $E_e = m_e c^2$ ) is the lightest known CEP with the largest known (absolute)charge-to-(rest)energy ratio in nature  $\phi_{\text{max}} = |e|/E_e$ , thus electromagnetic charge appears to cannot exist (and thus cannot manifest) without a minimum degree of spacetime curvature determined by  $E_e$  (which contributes to the energy tensor) and the almost infinitesimal Einstein's constant  $\kappa = 8\pi G/c^4 \left( \cong 2.1 \times 10^{-43} N^{-1} \right)$  (the coupling constant of Einstein's field equation).

Each of all known electromagnetically-charged elementary

particles (CEP) in the Standard model has a non-zero rest energy

#### 3.2 Second observation

There is a simple logarithmic function which appears to relate both  $\kappa$  and  $\phi_{
m max}$  to the fine-structure constant at rest

$$\alpha_0 = k_e q_e^2 / (\hbar c) (\cong 137^{-1})$$
 (with  $k_e = 1/(4\pi\varepsilon_0)$ 

 $\approx 8.99 \times 10^9 \, \text{Nm}^2 / \text{C}^2$  being the Coulomb's constant in vacuum measured at low non-relativistic energy scales) [5] which is the asymptotical minimum at rest of the electromagnetic running coupling constant  $\alpha(E) = \alpha_0 / (1 - \alpha_0 f(E))^{-1} [6]$ :

$$\alpha_0 \stackrel{99.92\%}{\cong} \left[ \log_2 \left( \kappa^{-1} k_e \phi_{\text{max}}^2 \right) \right]^{-1} \left( \cong 136.93^{-1} \right)$$
 (1)

scales 
$$E >> E_e$$
, with  $f(E) = \ln \left[ \left( E / E_e \right)^{2/(3\pi)} \right]$ , but uncertain validity

for energy scales close to Planck energy 
$$\,E_{Pl}^{}=\sqrt{\hbar c^5\,/\,G}\cong 10^{19} GeV$$

<sup>&</sup>lt;sup>1</sup> the leading log approximation of  $\alpha(E)$ , which is only valid for large energy

 $\alpha_0$  may be directly related to  $\left[\log_2\left(\kappa^{-1}k_e\phi_{\max}^2\right)\right]^{-1}$ the following numbered arguments and explanations:

- (1) As anticipated in the previous "Motivating points" sub-<mark>section of this paper</mark>, if the very large dimensionless physical constants (DPCs) (which are gravity-related in general, like  $\kappa^{-1}k_{\rho}\phi_{\rm max} \cong 10^{41}$  for example) are deeply related with the small DPCs (usually close to 1 and related to quantum mechanics, like  $\alpha_0$  for example), by any (yet unknown) mathematical function, then a logarithmic function (LF) would be the simplest (and thus the most natural) candidate solution of connecting these large and small DPCs, as other authors also considered in the past. Furthermore, even if it is not the case of such a logarithmical connection, possible LFs (connecting those DPCs) would still have to be ruled out first.
- (2) A direct logarithmic relation between an electromagnetic minimum of  $(\alpha_0)$  and an "electro-gravitational" maximum of nature  $\phi_{\text{max}}$  is quite intuitive;
  - (3)  $\kappa^{-1} \left( \cong 4.82 \times 10^{42} N \right)$  (which is relatively close to the

Planck force  $F_{Pl} = c^4 / G \cong 1.2 \times 10^{44} N$ ) may be interpreted as a global average "tension" of the spacetime fabric (as also interpreted by other authors [7]) which strongly opposes to any spacetime curvature (SC) induced by any source of energy (including electromagnetic and/or gravitational energy tensors): because of this resistance to any induced SC (by any rest energy and/or movement of any bosonic or fermionic EP),  $\kappa^{-1}$  is identified with the approximate value at rest of an (energy/length-)scale-dependent electro-gravitational resistivity of vacuum (EGRV) represented by R(E) with an asymptotic maximum

value at rest  $R_0 = \frac{2^{1/\alpha_0}}{k \phi^2} \left( \approx 5.19 \times 10^{42} N \right)$  (at zero-energy

scale  $E_0 = 0J$  which is physically unattainable, which makes  $R_0$ an asymptotical maximum) estimated to exactly correspond to the asymptotic minimum  $\alpha_0$  (which  $\alpha_0$  corresponds to the theoreticalonly energy scale  $E_0 = 0J$  for which  $f(E_0) = \ln(0)$  and  $\alpha_0 f(E_0) = \alpha_0 \ln(0)$  have no real value and  $\alpha(E) = \alpha_0 / (1 - \alpha_0 f(E))$  is "renormalizable"  $\alpha(E_0) = \alpha_0/1 = \alpha_0$  which obviously represents an asymptotical minimum), so that  $\alpha_0 = \left\lceil \log_2 \left( R_0 k_e \phi_{\text{max}}^2 \right) \right\rceil^{-1}$ . EGRV (measured by R(E) and  $R_0$  at rest) may be considered a truly fundamental parameter of spacetime with both c and G being EGRV. Another argument for  $\alpha_0$  measuring EGRV (which  $\alpha_0$  is alternatively defined as the probability of a real electron to emit or actually determined by R(E) and thus being indirect measures of

absorb a real photon) is that EGRV actually opposes to the photon emission process, in the sense that, for any real EP to emit a real photon, that photon first needs to overcome EGRV.

- (4) EGRV is very plausibly determined by the short-lived virtual particle-antiparticle pairs (VPAPs) emerging from the vacuum, which VPAPs interact with both photons and gravitational waves plausibly limiting their speed to a common maximum speedlimit for both speed of gravity and speed of light in vacuum. Charged EPs (composing charged VPAPs) interact much more strongly with photons than neutral EPs (composing neutral VPAPs) so that R(E) may actually depend on (and vary with) the ratio between the volumic concentrations of charged and neutral virtual EPs at various length scales of vacuum.
- (5) By replacing  $k_e \phi_{\rm max}^2$  with its equivalent  $\alpha_0 \hbar c / E_e^2$ ,  $lpha_0$  and  $R_0$  become related by a special type of exponential equation such as:

$$\left(\frac{1}{\alpha_0}\right)2^{1/\alpha_0} = \frac{R_0\hbar c}{E_e^2} \tag{2}$$

(6) Based on the previous equality,  $\alpha_0$  may also be considered as an indirect measure of EGRV and inversely redefined as the unique positive solution W of the exponential equation  $(1/w)2^{1/w} = C$ , with:

$$C = \frac{R_0 \hbar c}{E_e^2} \left( \stackrel{>}{\simeq} \frac{\kappa^{-1} \hbar c}{E_e^2} \right)$$
 (3)

(with  $R_0^{107.8\%} \cong \kappa^{-1}$  being the predicted asymptotic maximum of R(E) for unattainable zero-energy scale  $E = E_0 = 0J$ )

This equation can be solved by using the Lambert function only it to its converting natural-base (e) variant  $(\ln(2)/w)e^{\ln(2)/w} = C\ln(2)$  so that:

$$\alpha_0 = \frac{\ln(2)}{W(C\ln(2))} \tag{4}$$

(7) By considering  $\hbar$ ,  $E_e$  and c to all be (energy/length-) scale-invariant and based on  $\alpha(E) = \alpha_0/(1-\alpha_0 f(E))$ , we remind that Coulomb's constant  $k_e$  is not scale-invariant, but is actually variable with the energy/length scale and is currently defined in modern physics as a function of  $\alpha(E)$  such as  $k_e(E) = \alpha(E)\hbar c/e^2$  (with  $k_e = k_e(E_0) = \alpha_0\hbar c/e^2$ ) which is definition  $R_0 = \frac{2^{1.00}}{k_0 \phi_{...}^2}$ , R(E) can be inversely deduced and

generalized as 
$$R(E) = \frac{2^{1/\alpha(E)}}{k_e(E) \cdot \phi_{\text{max}}^2} = \frac{2^{(1-\alpha_0 f(E))/\alpha_0}}{\frac{\alpha_0 \hbar c / e^2}{(1-\alpha_0 f(E))} \cdot \frac{e^2}{E_e^2}}$$

with 
$$R_0 = R(E_0) = \frac{2^{1/\alpha_0}}{k_e \phi_{\text{max}}^2} = \frac{2^{1/\alpha_0}}{\left(\frac{\alpha_0 \hbar c}{e^2}\right) \frac{e^2}{E_e^2}} = \frac{2^{1/\alpha_0}}{\alpha_0 \hbar c / E_e^2}$$

$$R(E)$$
 can be further simplified to

$$R(E) = \frac{2^{1/\alpha_0 - f(E)}}{\frac{\alpha_0 \hbar c / E_e^2}{\left(1 - \alpha_0 f(E)\right)}} = \frac{2^{1/\alpha_0} / 2^{f(E)}}{\frac{\alpha_0 \hbar c / E_e^2}{\left(1 - \alpha_0 f(E)\right)}}$$
: the ratio in red from

be further simplified to 
$$R(E) = \frac{R_0 \left(1 - \alpha_0 f(E)\right)}{2^{f(E)}}$$
;  $\alpha_0$  was 
$$\ln(2)$$
 second in the same  $\ln(2)$  and is 
$$\ln(2)$$
 second in the same  $\ln(2)$  and is 
$$\ln(2)$$

redefined as equal to  $\frac{\ln(2)}{W(C\ln(2))}$  according to equation (4) and is

also roughly approximable to  $\alpha_0 \cong \frac{1}{\log_2(C)}$  which allows to

further simplify R(E) to a final form definable as:

$$R\left(E\right) = \frac{R_0}{2^{\mathrm{f(E)}}} \left[1 - \frac{\ln(2)f\left(\mathrm{E}\right)}{W\left(C\ln(2)\right)}\right] \cong \frac{R_0}{2^{\mathrm{f(E)}}} \left[1 - \frac{f\left(\mathrm{E}\right)}{\log_2\left(C\right)}\right]$$
(5)

This generalized  $R(E) = f(R_0)$  allows the generalization

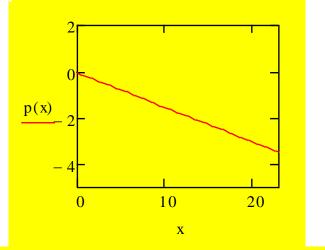
of 
$$C\left(=\frac{R_0\hbar c}{{E_e}^2}\right)$$
 to  $C(E)=\frac{R(E)\hbar c}{{E_e}^2}$ ;  $\alpha(E)$  can be also

 $C(E) = f \lceil R(E) \rceil$  such as:

$$\alpha(E) = \frac{\ln(2)}{W(\ln(2)C(E))} = \frac{\ln(2)}{W(\ln(2)R(E)\hbar c / E_e^2)}$$
 (6)

$$\left( \cong \frac{\alpha_0}{\left( 1 - \alpha_0 f(\mathbf{E}) \right)} \right)$$

The variation of the ratio  $p(x) = \log_{10} (R(10^x MeV) / R_0)$ (illustrating the variation of R(E) with the energy scale  $E = 10^x MeV$  in respect to  $R_0$ , which  $R_0$  is the asymptotical maximum of R(E)) is graphed next:



the previous R(E) formula is in fact  $R_0$  which allows R(E) to Figure 1. The graph of  $p(x) = \log_{10}(R(10^x MeV)/R_0)$ , for

 
 Table
 1.
 The comparative values
  $\alpha(E) = \frac{\ln(2)}{W(\ln(2)R(E)\hbar c / E_e^2)}$ approximation of  $\alpha(E) \left[ = \alpha_0 / (1 - \alpha_0 f(E)) \right]$ 

$E = 10$ MeV and various values of $x \in [0, 22]$						
$x \in [0, 22]$ and $E = 10^{x} MeV$	$\alpha(E) = \frac{\ln(2)}{W(\ln(2)R(E)\hbar c / E_e^2)}$	$\frac{\alpha(E)}{=\alpha_0/(1-\alpha_0 f(E))}$				
0 (E=1 MeV)	136.9 <sup>-1</sup>	136.9 <sup>-1</sup>				
5 (E=10 <sup>5</sup> MeV)	134.5 <sup>-1</sup>	134.5 <sup>-1</sup>				
10 (E=10 <sup>10</sup> MeV)	132-1	132 <sup>-1</sup>				
15 (E=10 <sup>15</sup> MeV)	129.6 <sup>-1</sup>	129.6 <sup>-1</sup>				
20 (E=10 <sup>20</sup> MeV)	127.1 <sup>-1</sup>	127.1 <sup>-1</sup>				

The prediction of a maximum allowed speed for any wave travelling in our universe and the graviton. Like  $R_0 \left( = R(E_0) \cong 5.19 \times 10^{42} N \right)$ , note that R(E) is measured in Newtons (force-units which can be expressed as Joule/meter thus linear energy density units): R(E) is thus the huge linear energy

density of the vacuum (expressed in J/m units and generated by the evancescent VPAPs which perpetually pop out from the vacuum and produce a huge tension in the spacetime fabric [7] measured by R(E)) which opposes to any gravitational or electromagnetic (transverse) wave propagating in the vacuum thus limiting the wavefront speed of those propagating physical waves to a maximum speed  $v_{\text{max}}$ : in Einstein's General relativity (**GR**), both the speed of the electromagnetic waves (photons) in vacuum (c) and speed of gravity  $(v_{\varrho})$  are stated to be upper-bounded and equal to  $v_{\text{max}}$ The largeness of R(E) indicates a very "rigid" spacetime (made so rigid by this huge inner tension, with its rigidness varying directproportionally with the length/size scale at which it is measured) which allows to be permeated only by waves with very small amplitudes (like in the case of the electromagnetic and gravitational transverse waves for example). No matter the nature of the physical wave (PW) travelling in the vacuum, this PW has to first attain a minimal momentum needed for it to produce at least a minimal deformation allowed by the hugely-tensioned spacetime fabric: in the case of electromagnetic waves (EMWs), this minimal (quantum angular) momentum is measured by Planck constant h; in the case of the gravitational waves (GWs), a minimal (needed) momentum  $h_{o}$  also very plausibly exists (as a sine-qua-non condition to surpass EGRV) and may actually be the quantum angular momentum of the hypothetical graviton (gr), which may have an energy scalar similar to the photon such as  $E_{gr} = h_g v$  (with vbeing the frequency of that hypothetical graviton). From the perspective of any straightly-traveling wavefront of any PW, spacetime can be regarded as an immense mesh of interwoven hugely-rigid (and relatively straight) strings (str) with (scaledependent) inner tension  $T_{str}(E) = R(E)$  and (scale-dependent) linear massic density  $\rho_{str}(E) = R(E)/c^2$  (measured in kg/m linear density units and the energy-mass conversion factor c [the speed of light in vacuum] being scale independent): the maximum allowed speed v<sub>max</sub> for any (low-amplitude) transverse wave

traveling on such a rigid string is given by the famous Galileo's formula  $v_{\text{max}} = \sqrt{\frac{T_{str}(E)}{\rho_{str}(E)}} \left( = \sqrt{c^2} = c \right)$  (which is only valid

for low-amplitude transverse waves, like EMWs and GWs actually are). In conclusion, R(E) measures the (scale-dependent) rigidness of the spacetime fabric (STF) and predicts the existence of a maximum speed  $v_{\rm max} \, (=c)$  for any PW traveling in this STF, but also the existence of minimal momentum for all EMWs (measured by h) and a distinct minimal momentum for all GWs (measured by the Planck-like gravitational quantum angular momentum  $h_g$  of the hypothetical graviton with energy-scalar

$$E_{gr} = h_g v).$$

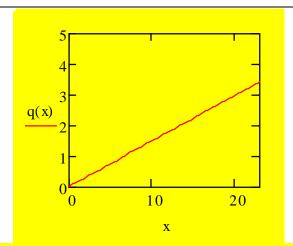
(8) Based on the approximate equality  $R_0^{107.8\%} \cong \kappa^{-1} \left(\frac{c^4}{8\pi G}\right)$ , an asymptotic minimum for big G (corresponding to the unattainable zero-energy scale) can be inversely deduced as  $G_0 = \frac{c^4}{8\pi R_0} \left(\cong 6.2 \times 10^{-11} m^3 kg^{-1} s^{-2} \cong 0.93 G\right)$ . Based on  $G_0 = f\left(R_0\right)$  we also propose a generalized quantum gravitational constant  $G_q\left(E\right)$  (which also varies with energy scale E) as derived from the same  $R\left(E\right)$ , also implying that big G may be actually a function of both the speed of light in vacuum  $\left(c\right)$  and speed of gravity  $v_g\left(=c\right)$  ( $c^4$  and  $v_g^4$  to be more specifically) and EGRV, such as:

$$G_q(E) = \frac{v_{\text{max}}^4}{8\pi R(E)} = \frac{c^4}{8\pi R(E)} = \frac{v_g^4}{8\pi R(E)}$$
 (7)

If the gravitational waves (carriers of the gravitational force/field) emitted by any physical body spread simultaneously in the four distinct dimensions of a 4D spacetime (as also stated by Einstein's general relativity), then it is quite intuitively for the gravitational coupling "constant"  $G_q(E)$  (which is argued here to be actually a composite "constant") to direct-proportionally depend on  $v_g^4(=c^4)$  and inverse-proportionally depend on the (scale-dependent) electro-gravitational resistivity of vacuum (EGRV) R(E) (which is an obstacle for those emitted gravitational waves to propagate any change in spacetime curvature and reach all their potential physical "targets").

From the previous relation, one may also note that any subtle variation of  $v_g$  and/or R(E) may produce a slight variation of big G numerical value: this fact may actually explain the apparently paradoxal divergence (with deviations up to  $\pm 1\%$ ) of big G experimental values despite the technical advances in the design of the modern experiments.

The variation of the ratio  $q(x) = \log_{10} \left( Gq \left( 10^x MeV \right) / G \right)$  (illustrating the variation of  $G_q(E)$  with the energy scale  $E = 10^x MeV$  in respect to  $G \left( \cong G_0 \right)$ , which  $G_0$  is the asymptotical minimum of  $G_q(E)$ ) is graphed next:



**Figure 2.** The graph of  $q(x) = \log_{10} \left( Gq \left( 10^x MeV \right) / G \right)$ , for integer  $x \in [0, 22]$ , with  $x \cong 22$  for Planck energy  $E_{Pl} = \sqrt{\hbar c^5 / G} \cong 10^{22} MeV$ 

**Table 2.** The predicted values of  $G_q(E) = \frac{c^4}{8\pi R(E)}$  for  $E = 10^x MeV$  and various values of  $x \in [0, 22]$ 

$x \in [0, 22]$	$G_q(E)/G$
and $E = 10^x MeV$	
0 (E=1 MeV)	1.025
5 (E=10 <sup>5</sup> MeV)	<b>5.7</b>
10 (E=10 <sup>10</sup> MeV)	31.4
15 (E=10 <sup>15</sup> MeV)	174.2
20 (E=10 <sup>20</sup> MeV)	965.7
22 (E=10 <sup>22</sup> MeV=E <sub>Pl</sub> )	1916

Final note of this 1st paper section. It is important to remember that R(E),  $\alpha(E) = \frac{\ln(2)}{W(\ln(2)R(E)\hbar c/E_e^2)}$  and  $G_q(E) = \frac{c^4}{8\pi R(E)}$  were all deducted starting from the leading log approximation (LLA) of  $\alpha(E) \Big[ = \alpha_0/\big(1-\alpha_0f(E)\big) \Big]$ , which has uncertain validity for energy scales close to Planck energy  $E_{Pl} \Big( \cong 10^{19} \, GeV \Big)$  and that is why R(E),  $\alpha(E) \Big[ = f(R(E)) \Big]$  and  $G_q(E)$  also have uncertain validity for energy scales close to  $E_{Pl}$ : we argue that the zero-energy hypothesis (ZEH) proposed next may significantly help in solving this "bothering" uncertainty of LLA (which uncertainty is still a big problem of quantum electrodynamics) and also correct R(E) and  $G_q(E)$  values for large energy scales  $E \cong E_{Pl}$ 

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# II. A zero-energy hypothesis (ZEH) applied on virtual particle-antiparticle pairs (VPAPs)

We also propose a zero-energy hypothesis (**ZEH**) applied on any virtual particle-antiparticle pair (**VPAP**) popping out from the quantum vacuum at hypothetical length scales comparable to Planck scale. ZEH can be regarded as an extension of the notorious zero-energy universe hypothesis first proposed by the theoretical physicist Pascual Jordan [8], assuming minimal curvature (thus almost flat spacetime) at Planck scale. Presuming the gravitational and electrostatic inverse-square laws to be valid down to Planck scales and considering a VPAP composed from two electromagnetically-charged EPs (**CEPs**) each with non-zero rest mass  $m_{EP}$  and energy  $E_{EP} = m_{EP}c^2$ , electromagnetic charge  $q_{EP}$  and negative energies of attraction  $E_g = -Gm_{EP}^2/r$  [9] and  $E_q = -k_e \left| q_{EP} \right|^2/r$ , ZEH specifically states that:

$$2E_{EP} + E_g + E_q = 0 (8$$

Defining the ratios  $\phi_g = G/r$  and  $\phi_e = k_e/r$  the previous equation is equivalent to the following simple quadratic equation with unknown  $x = m_{EP}$ :

$$\phi_g x^2 - (2c^2)x + \phi_e q_{EP}^2 = 0 (9$$

The previous equation is easily solvable and has two possible solutions which are both positive reals if  $c^4 \ge \phi_g \phi_e q_{EP}^{\ \ 2} \ge 0$ :

The realness condition  $c^4 \ge \phi_e \phi_e q_{EP}^2 \ge 0$  implies the

$$m_{EP} = x = \frac{c^2 \pm \sqrt{c^4 - \phi_g \phi_e q_{EP}^2}}{\phi_g}$$
 (10)

existence of a minimum distance between any two EPs (composing the same VPAP)  $r_{\min} = q_{EP} \sqrt{Gk_e} / c^2 \cong 10^{-1} l_{Pl}$  (for  $q_{EP(\cong e)} \in \{e, \pm \frac{1}{3}e, \pm \frac{2}{3}e\}$  and with  $l_{Pl}$  being the Planck length): obviously, for distances lower than  $r_{\min}$  the previous equation has only imaginary solutions  $x = m_{EP}$  for any charged EP; by this fact, ZEH offers a new interpretation of the Planck length, as being the approximate distance under which charged EPs cannot have rest masses/energies valued with real numbers; because  $k_e$  is actually variable with the energy/length scale and currently defined as a function of  $\alpha(E)$  such as  $k_e(E) = \alpha(E)\hbar c/e^2$ ,  $r_{\min}$  can be generalized as  $r_{\min}(E) = (q_{EP}/e)\sqrt{G\alpha(E)\hbar c}/c^2$  (and can slightly vary as

such). Note that  $r_{\min}$  can be additionally corrected to include the strong force (implying color charge) and/or weak force (implying weak charge) between any quark (or gluon, or lepton coupling with the weak field) and its antiparticle (composing the same VPAP): however, these potential corrections are estimated to only slightly modify  $r_{\min}\left(E\right)$  values so that they're not detailed this paper.

(1) non-zero positive values  $m_{EP} = \left(c^2 + \sqrt{c^4}\right) / \phi_g = 2c^2 / \phi_g \left(> 0 \text{ kg}\right) \text{ (like in the case of all three types of neutrinos, the Z boson and the Higgs boson) AND}$ 

(2) zero values  $m_{EP} = \left(c^2 - \sqrt{c^4}\right)/\phi_g = 0\,kg$  (like in the case of the gluon and the photon which both have zero rest mass  $m_{EP} \left(=0kg\right)$  and are assigned only relativistic mass/energy by the Standard model).

**Important remark**. In other words, formula (**10**) allows NEPs to be divided in two major families (NEPs with non-zero rest mass and NEPs possessing only relativistic mass) which is an indirect proof that  $m_{EP}$  is a function of  $q_{EP}$  (as requested/imposed by  $q_{EP}$ ) and *not* vice-versa, as if the  $q_{EP}$  quantum also imposes fixed/discrete gradients  $\Delta m = m_{EP(2)} - m_{EP(1)} (\geq 0 \, kg) = f \left( q_{EP} \right)$  between various types of EPs. ZEH additionally states that the two conjugated elementary

mass solutions  $m_{EP} = \left(c^2 \pm \sqrt{c^4 - \phi_g \phi_e q_{EP}^2}\right)/\phi_g$  (of ZEH's main equation) actually define a boson-fermion pair (with conjugated masses) called here "conjugated boson-fermion pair" (CBFP). ZEH actually conjectures a new type of boson-fermion symmetry/"mass-conjugation" based on ZEH's main quadratic equation (with partially unknown coefficients): ZEH mainly predicts two distinct types of massless neutral fermions (modelled as conjugates of the Higgs boson and Z boson respectively) with zero charge and zero rest mass (which, implicitly, don't couple electromagnetically and gravitationally and thus may be plausibly the main constituents of dark matter and dark energy), a bijective mass-conjugation between the three types of neutrinos and the massless bosons (gluon, photon and the hypothetical graviton) and a relation of mass-conjugation between the electron/positron and the W<sup>±</sup> boson (see next).

For the beginning, let us start to estimate the values of  $\phi_g$  for the known electromagnetically-neutral EP (**NEP**). For  $q_{EP}=0$ , the conjugated solutions expressed by formula (10) simplify for any

NEP such as 
$$m_{NEP} = \left(c^2 \pm c^2\right)/\phi_g$$
, resulting  $\phi_{g(NEP)} = \left(c^2 \pm c^2\right)/m_{NEP}$ .

Focusing on Higgs boson and Z boson and their ZEHpredicted correspondent/conjugated massless fermions. In a first step and defining the unit of measure of  $\phi_{g} \left( = 2c^{2} / m_{nFP} \right)$  as  $u = m^2 kg^{-1}s^{-2}$ , ZEH directly estimates  $\phi_g$  for the Z boson (**Zb**) and Higgs boson (Hb) (with both Zb and Hb having non-zero rest such as  $\phi_{g(Z_b)} (= 2c^2 / m_{Z_b}) \cong 10^{42} u$ energies)  $\phi_{g(Hb)} = 2c^2 / m_{Hb} \cong 8 \times 10^{41} u$ . ZEH states that both Zb and Hb have two distinct correspondent/conjugated massless neutral fermions formally called the "Z fermion" (Zf) (which shares the same  $\phi_{g(Zb)} (\cong 10^{42} u)$  with Zb) and the "Higgs fermion" (**Hf**) (which shares the same  $\phi_{g(Hb)} (\cong 8 \times 10^{41} u)$  with Hb) with zero masses  $m_{Zf} = (c^2 - c^2)/\phi_{g(Zh)} (= 0 kg)$  $m_{Hf} = (c^2 - c^2)/\phi_{\alpha(Hh)} (= 0 kg)$  (thus both moving with the speed of light in vacuum and possessing only relativistic masses instead of rest masses). Based on the previously defined  $r_{\min} \left( \cong 10^{-1} l_{Pl} \right)$ obtain  $G_{Zb(\min)} \left( = \phi_{g(Zb)} r_{\min} \right) \cong G_{Hb(\min)} \left( = \phi_{g(Hb)} r_{\min} \right) \cong 2 \times 10^{16} G$ : based on these huge predicted lower bounds for big G values at Planck scales, ZEH states that  $E_{arrho}$  may reach the same magnitude as  $E_a$   $\left(E_g \cong E_a \Leftrightarrow \phi_g m_{FP}^2 \cong \phi_e q_{FP}^2\right)$  at scales comparable to Planck scale and that R(E) (thus lpha(E) and  $G_a(E)$ ) may actually take discrete values only. Additionally, ZEH helps correcting the previously defined  $G_a(E)$  by assigning it values much larger than the previously  $G_q \left(10^{22} MeV 
ight) = 1916 \cdot G$  at scales comparable to  $r_{\min}$  .

Focusing on all three types of neutrinos, photon, gluon and hypothetical graviton. In a second step, ZEH estimates the lower bounds of  $\phi_g$  for all known three neutrinos, as deducted from the currently estimated upper bounds of the non-zero rest energies of all three known types of neutrino: the electron neutrino (en) with  $E_{en} < 1eV$  [10], the muon neutrino (mn) with  $E_{mn} < 0.17 MeV$  [11] and the tau neutrino (tn) with  $m_{tn} < 18.2 MeV$  [12] [13]:  $\phi_{g(en)} > 10^{53} u$ ,  $\phi_{g(mn)} > 6 \times 10^{47} u$  and  $\phi_{g(tn)} > 6 \times 10^{45} u$ , with  $\phi_{g(en)}$  being assigned a very large

big G lower bound  $G_{en(\min)} \left(=\phi_{g(\text{en})}r_{\min}\right) \cong 2 \times 10^{28} G$  thus strengthening the previously introduced (sub-)hypothesis  $\phi_g m_{EP}^{\ \ 2} \cong \phi_e q_{EP}^{\ \ 2}$  at scales close to Planck scale. **Remark**. It is easy to observe that ZEH generally predicts progressively larger "real" big G values for progressively smaller  $m_{EP}$ : an additional explanation for this correlation shall be offered later in this paper. We must also remind that a specific virtual EP (**VEP**) may have a variable mass lower or equal to the mass  $m_{EP}$  of the real "version" of the same EP  $\left(m_{VEP} \leq m_{EP}\right)$  and that is why the "virtual" big G values assigned to the gravitational field acting between a virtual particle and its antiparticle (part of the same VPAP) may be even larger than the previously calculated ones.

ZEH cannot directly estimate the values of  $\phi_{g(nEP)}$  for the massless photon (**ph**)  $\phi_{g(ph)}$  and the gluon (**gl**)  $\phi_{g(gl)}$  due to the division-by-zero error/paradox. However, ZEH additionally states that  $\phi_{g(ph)}$  and  $\phi_{g(gl)}$  may have very large values coinciding with  $\phi_{g(en)}$ ,  $\phi_{g(mn)}$  and  $\phi_{g(gl)}$ . More specifically, ZEH speculates that  $\phi_{g(ph)} > \phi_{g(gl)}$  and that there also exists a massless graviton (**gr**) defined by  $\phi_{g(gr)} > \phi_{g(ph)} \left( > \phi_{g(gl)} \right)$  so that:  $\phi_{g(gr)} = \phi_{g(en)}$ ,  $\phi_{g(ph)} = \phi_{g(mn)}$  and  $\phi_{g(gl)} = \phi_{g(m)}$ .

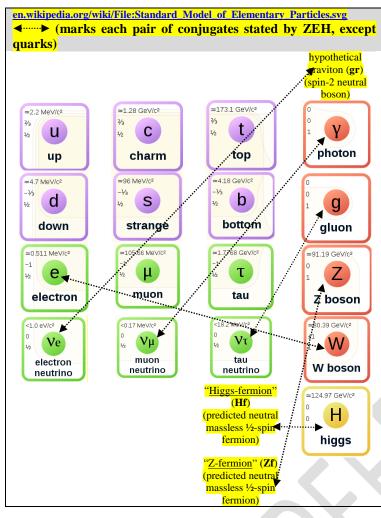
Focusing on the electron-W boson conjugated pair. In a third step, ZEH additionally states that the W boson and the electron also form a conjugate boson-fermion pair with rest masses  $m_e = \left(c^2 - \sqrt{c^4 - \phi_{g(W/e)}\phi_{e(W/e)}\phi_{e(W/e)}q_e^2}\right)/\phi_{g(W/e)}$  and  $m_W = \left(c^2 + \sqrt{c^4 - \phi_{g(W/e)}\phi_{e(W/e)}\phi_{e(W/e)}q_e^2}\right)/\phi_{g(W/e)}$ . The common term  $\sqrt{c^4 - \phi_{g(W-e)}\phi_{e(W-e)}q_e^2}$  of both rest masses  $(m_e \text{ and } m_W)$  disappears when summing  $m_e + m_W = 2c^2/\phi_{g(W/e)}$ , from which their common/shared  $\phi_{g(W/e)}$  ratio can be reversely estimated as  $\phi_{g(W/e)} = 2c^2/\left(m_e + m_W\right) \cong 1.25 \times 10^{42}u$ , which is relatively close to  $\phi_{g(Zb)}\left(\cong 10^{42}u\right)$  and  $\phi_{g(Hb)}\left(\cong 8 \times 10^{41}u\right)$ . The other  $\phi_{e(W/e)}$  ratio can be also reversely estimated from both  $m_W$  (or  $m_e$ ) and  $\phi_{g(W/e)}$  as  $\phi_{e(W/e)}\cong 6.4 \times 10^{24}F^{-1}$ .

big G lower bound  $G_{en(\min)} \left( = \phi_{g(\text{en})} r_{\min} \right) \cong 2 \times 10^{28} G$  thus strengthening the previously introduced (sub-)hypothesis  $\phi_g$  and  $\phi_e$  ratios).

Table 1. The noise of conjugated EDs westisted by 7EH					
Table 1. The pair of conjugated EPs predicted by ZEH					
Boson (/corresponde	(/corresponde	The second secon	1		
		shared $\phi_g$	shared $\phi_e$		
nt conjugate	nt conjugate	ratio of a	ratio of a		
boson of a	fermion of a	conjugated	conjugated		
known	known boson)	boson-fermion	boson-fermion		
fermion)		pair	pair		
	Non-guark EPs s	as treated by ZEH			
hypothetical	electron		?		
graviton ( <b>gr</b> )	neutrino (en)	$\phi_{g(gr)} = \phi_{g(en)}$	•		
(spin-2 neutral	ilcutilio ( <b>eli</b> )	(			
boson)		$(>1.1\times10^{53}u)$			
boson)					
photon ( <b>ph</b> )	muon noutrino				
(spin-1 neutral	muon neutrino	$\phi_{g(ph)} = \phi_{g(mn)}$	?		
	(mn)				
<mark>boson)</mark>		$(>6\times10^{47}u)$			
		(			
1 (1)			0		
gluon (gl)	tauon neutrino	$\phi_{g(gl)} = \phi_{g(tn)}$	<mark>?</mark>		
(spin-1 neutral	(tn)				
boson , with		$(>5.6\times10^{45}u)$			
color charge		(			
only)					
Z boson ( <b>Zb</b> )	"Z-fermion"	4	?		
(spin-1 neutral	$(\mathbf{Zf})$	$\phi_{g(Zb)}$	-		
boson)	(predicted	$\approx 10^{42} u$			
Cosony	neutral	= 10 u			
	massless ½-				
	spin fermion)				
Higgs boson	"Higgs-	<u> </u>	<mark>?</mark>		
( <b>Hb</b> )	fermion" (Hf)	$\phi_{g(Hb)}$	<u>.</u>		
(spin-0/scalar	(predicted	$\approx 8 \times 10^{41} u$			
neutral boson)	neutral	$\approx 8 \times 10^{12} u$			
neatrar boson)	massless ½-				
	spin fermion)				
	spin termion)				
W boson	electron (e)	$\phi_{g(W/e)} \cong$	$\phi_{e(W/e)} \cong$		
(Wb)					
(spin-1		$1.25 \times 10^{42} u$	$6.4 \times 10^{24} F^{-1}$		
<mark>charged</mark>					
<mark>boson)</mark>					

All the proposed pairs of EP-conjugates (as stated by ZEH) are also illustrated in the **next table**: as it can be seen from this next table, ZEH transforms the already "classical" 2D table of EPs (from the Standard model [SM] of particle physics) in a 3D structure/table in which EPs are grouped *not only* in boson and fermion families/subfamilies, BUT they are also grouped and inter-related by an "underneath" relation of boson-fermion mass conjugation, all based on the same simple semi-empirical quadratic equation proposed by ZEH.

<u>Table 2</u>. The pairing of conjugated EPs predicted by ZEH and marked by interconnecting arrows. Source of image extracts:



In a checkpoint conclusion, ZEH has the potential to explain the non-zero rest masses of 12 known and hypothetical EPs (Zb & Zf, Hb & Zf, gr & en, ph & mn, gl & tn, Wb & electron) plus their antiparticles by only seven discrete ratios:  $\phi_{g(Zb)} \left(=\phi_{g(Zf)}\right)$ ,  $\phi_{g(Hb)} \left(=\phi_{g(Hf)}\right)$ ,  $\phi_{g(gr)} \left(=\phi_{g(en)}\right)$ ,  $\phi_{g(gh)} \left(=\phi_{g(mn)}\right)$ , and  $\phi_{g(W/e)} \left(\&\phi_{e(W/e)}\right)$ .

ZEH uses the predicted minimum length/distance  $r_{\min}\left(=\left|q_{EP}\right|\sqrt{Gk_e}\,/\,c^2\cong10^{-1}l_{Pl}\right)$  needed for any virtual particle-antiparticle pair (**VPAP**) to pop out from the vacuum at the first place (as stated and predicted by ZEH for all rest masses to be describable by real numbers with mass units) and all the ZEH-predicted  $\phi_g$  and  $\phi_e$  ratios (briefly listed in the first table of this paper) to predict (**pr.**) the big G and Coulomb's constant  $k_e$  values at scales  $r_{\min}\left(\cong10^{-1}l_{Pl}\right)$  comparable to Planck scale as  $G_{pr}=\phi_{g(pr)}r_{\min}$  and  $k_{e(pr)}=\phi_{e(pr)}r_{\min}$  (see the next table)

_						
	Table 3. The predicted big G values $G_{pr} = \phi_{g(pr)} r_{\min}$ and					
	Coulomb's constant values $k_{e(pr)} = \phi_{e(pr)} r_{\min}$ for all pairs of					
	conjugated EPs predicted by ZEH.					
ĺ	Pair of Common/ $G_{pr}$ $k_{e(pr)}$					
	<mark>conjugated</mark>	shared $\phi_{_{\mathcal{Q}}}$	<u> </u>	1		
	<b>EPs</b>	and $\phi_e$ ratios	$\left(=\phi_{g(pr)}r_{\min}\right)$	$\left(=\phi_{e(nr)}r_{\min}\right)$		
		and $\varphi_e$ ratios	( 8(p) 111111)			
ŀ	Non-quark EPs as treated by ZEH					
ľ	hypothetical			?		
	graviton ( <b>gr</b> )	$\phi_{g(gr)} = \phi_{g(en)}$	$> 2.1 \times 10^{27} G$			
	& electron	$(>1.1\times10^{53}u)$	> 2.1×10 ° O			
	neutrino (en)	(* 1111113 21)				
	1 / 1	?	222	0		
	photon ( <b>ph</b> ) - muon neutrino	$\phi_{g(ph)} = \phi_{g(mn)}$	$> 1.2 \times 10^{22} G$	<mark>?</mark>		
	(mn)	( = 1047)	(the same for			
	(1111)	$(>6\times10^{47}u)$	all photons, no			
		?	matter their			
ŀ	gluon ( <b>gl</b> ) -	1 1	frequency)			
	tauon neutrino	$\phi_{g(gl)} = \phi_{g(tn)}$	$>1.2\times10^{20}G$	<u>-</u>		
	(tn)	$(>5.6\times10^{45}u)$	>1.2×10 G			
		$(>3.0\times10^{\circ} u)$				
		?				
	Z boson ( <b>Zb</b> )	$\phi_{g(Zb)}$	$\approx 2.1 \times 10^{16} G$	<mark>?</mark>		
	<mark>&amp; "<u>Z-</u></mark>		_ 2.17.10 0			
	fermion" (Zf)	$\approx 10^{42} u$				
4	<mark>Higgs boson</mark>	$\phi_{g(Hb)}$	$\cong 1.7 \times 10^{16} G$	?		
	( <b>Hb</b> ) &					
	"Higgs-	$\approx 8 \times 10^{41} u$				
1	fermion" (Hf)					
	W boson	$\phi_{g(W/e)} \cong$				
1	(Wb) &	_	$\approx 2.6 \times 10^{16} G$	$\cong 10^{-21} k_{\varrho}$		
,	electron (e)	$1.25 \times 10^{42} u$		e		
,		$\phi_{\mathrm{e(W/e)}} \cong$				
١	1	$6.4 \times 10^{24} F^{-1}$				

Interpretation. From the previous table, one can easily remark that ZEH predicts a big G which may increase (when decreasing the length scale of measurement up to values  $G_{pr}\left(=\phi_{g(\mathrm{en})}r_{\min}\right)>2.1\times10^{27}\,\mathrm{G}$  at  $r_{\min}\left(\cong10^{-1}l_{Pl}\right)$  length scales (comparable to Planck scale): concomitantly (and accordingly to the same table) and interestingly, ZEH predicts that Coulomb's constant  $k_e$  may drop down to values  $k_{e(pr)}\left(=\phi_{e(\mathrm{W/m})}r_{\min}\right)\cong10^{-21}k_e$  at the same length scales close to  $r_{\min}\left(\cong10^{-1}l_{Pl}\right)$ . Important observation. For the electron rest mass  $m_e$  at macroscopic scales  $m_e$  (for

which 
$$G_{pr}\cong G$$
) for example, the  $\frac{k_eq_e^2}{Gm_e^2}\Big(\cong 4.2\times 10^{42}\Big)$ 

dimensionless ratio reaches almost 43 orders of magnitude (in favor of the  $k_e q_e^{\ 2}$  numerator): interestingly, at Planck (PI) scales the ZEH-predicted big G may grow by at least 27 orders of magnitude (up to  $G_{\rm Pl} \cong 10^{27} \, G$ ) and  $k_e$  may drop by at least 21 orders of magnitude (down to  $k_{e(Pl)} \cong 10^{-21} k_e$ ) which may bring the ratio

$$\frac{k_{e(\text{Pl})}q_e^2}{G_{\text{Dl}}m_e^2}$$
 relatively close to 1; the Coulomb's constant  $k_e$  is

currently defined as a function of the running coupling constant of the electromagnetic field (EMF)  $\alpha(E) = \alpha_0 / (1 - \alpha_0 f(E))$  so that  $k_e(E) = \alpha(E)\hbar c/q_e^2$ : the currently known  $\alpha(E)$  (which is

currently predicted by its leading log approximation [LLA] to can only grow when approaching Planck energy/length scales  $\,E_{Pl}^{}\,)$  is thus alternatively predicted by ZEH to actually slightly grow (as described by LLA) at first (when decreasing the length scale) but then to drop significantly down to  $\alpha_{Pl} = \alpha(E_{Pl})$  so that

$$k_{e(Pl)} = \alpha_{Pl} \hbar c / q_e^2 \left( \cong 10^{-21} k_e \right)$$
 which is equivalent to  $\alpha_{Pl} \cong 10^{-21} \alpha_0$  (which tends to the value of the *gravitational*

coupling constant 
$$\alpha_G = \frac{Gm_e^2}{\hbar c} \cong 10^{-45} \cong 10^{-43} \cdot \alpha_0$$
) and

indicates EMF to probably possess asymptotic freedom (like the strong nuclear field was already proved to have). Based on the previous observation, ZEH additionally states (and predicts) that the gravitational field (GF) progressively grows in strength when  $r_{\min} \left( \cong 10^{-1} l_{Pl} \right)$  length-scale (up to approaching the  $G_{\rm DI} > 10^{27} G$ ) and the electromagnetic field (EMF) slightly

grows (as described by LLA) and then drops in strength (when approaching the same  $r_{\min}$ length-scale) down  $k_{e(Pl)} < 10^{-21} k_e$  and  $\alpha_{Pl} \cong 10^{-21} \alpha_0$  reaching the following

equality at  $r_{\min}$  scales:

$$G_{Pl}m_e^2 \cong k_{e(Pl)}q_e^2 (\cong m_e c^2 r_{\min})$$
 (11)

The previous equation is essentially a fundamental principle of electro-gravitational strength balance/symmetry at Planck scales, a principle which allows (as a sine-qua-non condition added to Heisenberg's uncertainty principle) the existence of virtual particleantiparticle pairs (VPAPs) from the first place.

particle-antiparticle pair (VPAP) to pop out from the vacuum at the first place (as stated and predicted by ZEH for all rest masses to be describable by real numbers with mass units) to predict a series of 'practical" (**pr.**) radii  $\left(r_{pr}\right)$  needed for each known/unknown point-like EP (to pop out as a VPAP in the first place) and a finite maximum allowed massic/energetic density in our universe (**OU**).

For big G values to grow progressively with a decreasing length

scale  $r_{nr}$ , ZEH proposes/conjectures that both the very large (but finite!) maximum  $G_{\text{max}} = G_{Pl} \left( > 2.1 \times 10^{27} G \right)$  and very small (but finite!)  $r_{\min} \left( \cong 10^{-1} l_{Pl} \right)$  bijectively correspond only to the electron neutrino (en) (with very small BUT finite rest mass  $m_{en} < 1eV/c^2$ ) which thus generates a conjectured maximum (large but finite!) allowed (3D spherical) "practical" massic density in our universe (OU) identified with the massic density of en (which has a predicted lower bound significantly smaller than Planck density  $\rho_{Pl} = m_{Pl} / l_{Pl}^{3} \cong 10^{96} \text{kg m}^{-3}$ ):

$$\rho_{OU(\text{max})} = \rho_{en} \left( \cong \frac{m_{en}}{\frac{4\pi}{3} r_{\text{min}}^{3}} \right) > 1.6 \times 10^{71} kg \, m^{-3} (12)$$

Furthermore, ZEH ambitiously (and additionally) conjectures that the pre-Big-Bang singularity (pBBS) was not infinitely dense (thus wasn't a true gravitational singularity with infinite density!) had a large-but-finite density  $\rho_{en} \left( > 1.6 \times 10^{71} kg \, m^{-3} \right)$  OR in the  $\left[ \rho_{en}, \rho_{Pl} \right]$ interval, thus being a quasi-singularity with  $ho_{pBBS} = 
ho_{OU(max)}$ 

or  $ho_{pBBS} \in \left[
ho_{en}, 
ho_{Pl}
ight]$  with all known/unknown EPs being redefined as remnant "crocks" of this pBBS and sharing

$$\rho_{EP} \cong \rho_{pBBS} \left( = \rho_{OU(\text{max})} \right)$$
 (ZEH's unique-density conjecture UDC)).

Based on the previously defined UDC, ZEH also proposes a simple formula for calculating the practical radii  $r_{pr(EP)}$  of any known type of known/unknown EP with non-zero rest mass:

$$r_{pr(EP)} \stackrel{>}{=} r_{\min} \sqrt[3]{m_{EP} / m_{en}}$$
 (13)

For example, the previously formula predicts that the Higgs boson (Hb) has a practical radius with a lower bound defined by  $r_{pr(Hb)} \cong r_{min} \sqrt[3]{m_{Hb}/m_{en}} \cong 5 \times 10^3 r_{min}$ , with all the other known/unknown EPs with non-zero rest masses smaller than  $m_{HP}$ having their practical radii approximately in the closed interval

ZEH also states that known/unknown EPs with non-zero rest masses larger than  $m_{en}$  and practical radii larger than  $r_{\min}$  correspond to smaller big G values  $G_{EP} < G_{\max} \left( = G_{Pl} \right)$ ; more specifically, ZEH actually proposes the following generalizations for any neutral or charged EP:

$$G_{EP}m_{EP}^{2} \cong 2m_{EP}c^{2}r_{\text{pr(EP)}}$$
(for neutral EPs)

$$G_{EP}m_{EP}^{2} \cong k_{e(EP)}q_{EP}^{2} \left(\cong m_{EP}c^{2}r_{pr(EP)}\right)$$
 (15)

Based on the previous two equations, the big G values corresponding to each length-scale measured by each practical radii in part (of each type of EP in part) can be reversely deduced as:

$$G_{EP} \cong \frac{2c^2}{m_{EP}} r_{\text{pr(EP)}} \cong \frac{2c^2 r_{\min}}{m_{EP}} \sqrt[3]{\frac{m_{EP}}{m_{en}}}$$
(16)
(for neutral EPs)

$$G_{EP} \cong \frac{c^2}{m_{EP}} r_{\text{pr(EP)}} \cong \frac{c^2 r_{\min}}{m_{EP}} \sqrt[3]{\frac{m_{EP}}{m_{en}}}$$
(17)

To illustrate the growth of  $G_{EP}$  with the decrease in the length scale measured by  $r_{\rm pr(EP)}$  ZEH proposes the double-logarithmic

ratio 
$$f_{EP} = \log_{10} \left( \frac{\log_{10} (G_{EP} / G)}{r_{pr(EP)} / r_{min}} \right)$$
 which is graphed next.

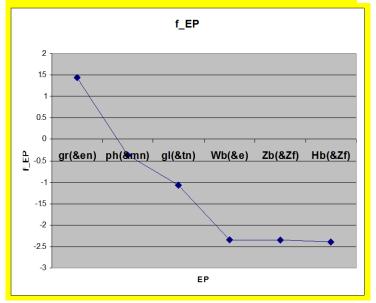


Figure 3. The variation of  $f_{EP}$  with  $r_{pr(EP)}$  which illustrates the increase of big G  $(G_{EP})$  values when the practical radius  $r_{pr(EP)}$  (of each EP type in part) decreases, with all previously discussed EPs being arranged in the ascending order of their  $r_{pr(EP)}$  values (from left to right). The rhombic blue points from this graph (indirectly) correspond to each  $G_{EP}$  value (assigned to each type of EP) and the slopes of the segments between each any two adjacent points (indirectly) correspond to each  $\phi_{g(EP)}$  (assigned to the EP that corresponds to the left rhombic point of each segment in part).

These new large  $G_{EP}$  values integrate with  $G_q(E)$  (and corrects it in the Planck domain), which  $G_q(E)$  grows in a smooth manner from macroscopic scales down to scales close to (but larger than)  $r_{pr(Hb)} = 5 \times 10^3 r_{\min}$ , but then grows abruptly and in a quantum saltatory manner (by a set of discrete slopes  $\phi_{g(EP)} = G_{EP} / r_{pr(EP)}$ ) in the approximate  $\begin{bmatrix} r_{\min}, r_{pr(Hb)} \end{bmatrix}$  interval, probably because a granular structure of spacetime in that closed interval  $\begin{bmatrix} r_{\min}, r_{pr(Hb)} \end{bmatrix}$ .

In a checkpoint conclusion, the zero/non-zero discrete values of rest masses of known and unknown EPs

$$\left(m_{EP} = \frac{c^2 \pm \sqrt{c^4 - \phi_g \phi_e q_{EP}^2}}{\phi_g}\right)$$
 are all stated by ZEH to be

actually generated by the quantized electromagnetic charge and by the discrete values of R(E) and  $G_q(E)$  implicitly in the subdomain of length scales  $\begin{bmatrix} r_{\min}, r_{\text{pr}(Hb)} \end{bmatrix}$ , a quantization/discreteness probably determined by a granular structure of spacetime in that sub-domain of length scales.

Focusing on the three generations of quarks and both the muon and the tauon. ZEH may deal with the known quarks and the muon plus tauon (which are considered two distinct excited states of the electron) in multiple ways, all speculative however:

(1) Each quark in part may have its own correspondent boson mass-conjugate (named here "quark-boson", because its has the same fractional charge as its mass-conjugate quark); however, ZEH-3a doesn't allow to directly estimate the  $\phi_g$  and  $\phi_e$  ratios for each (quark-)boson-quark pair, because the true existence of these theoretical quark-bosons (and their rest masses) is uncertain: the possible existence of quark bosons (with fractional charge) obviously implies the possible existence of additional "exotic" fundamental physical forces/fields still unknown in the present. If the ZEH's mass-conjugation principle wouldn't apply to quarks (which is probably not the case), the discrete values of  $\phi_g$  for all the other (charged) EPs with  $q_{EP} = f \cdot e$  ( $m_{EP} = x$  and  $f \in \{\pm 1, \pm \frac{1}{2}, \pm \frac{1}{2}\}$ ) could have been easily determined by using the previously introduced additional statement of ZEH

 $\left(\phi_{g}m_{EP}^{2} \cong \phi_{e}q_{EP}^{2}\right)$  which simplifies the initial equation (9) which becomes  $\phi_g x^2 - (2c^2)x + f^2\phi_g x^2 = 0$  (which, by dividing both left and right terms with  $x \neq 0$  becomes equivalent to  $(1+f^2)\phi_g x - (2c^2) = 0$  and  $(1+f^2)\phi_g x = 2c^2$  and allows the estimation of  $\phi_g \cong \frac{2c^2}{(1+f^2)m_{ER}}$  as approximately  $\phi_g \cong 2c^2/(2m_{FP}) \cong c^2/m_{FP}$  for all known |e|-charged leptons (with  $f = \pm 1$ ), with slight variations in the case of quarks (depending on the exact fractional charge of those quarks):  $\phi_q \cong 2c^2/(\frac{13}{9}m_{EP})$  (in the case of  $\frac{2}{3}|e|$ -quarks) and  $\phi_{e} \cong 2c^{2}/(10\% m_{EP}) \cong c^{2}/(5\% m_{EP})$  in the case of  $\frac{1}{3}|e|$ (2) Quarks with the same fractional charge however (which are aligned horizontally in the particles table of the Standard model), may be actually conjugated in fermion-fermion (quark-quark) pairs like up-charm pair (of conjugates) quarks (uq-cq), down-strange pair of quarks (dq-sq), top-"X\_top" pair of quarks (tq-Xtq) and bottom-"X\_bottom" pair of quarks (bq-Xbq) pair, with the herenamed "X top" quark (with electromagnetic charge [emc]  $\pm 2/3e$ ) and "X\_bottom" quark (with emc ±1/3e) actually forming a 4<sup>th</sup> generation of quarks (which is still a subject of active research at the LHC today and was first predicted by Sheldon Lee Glashow and James Bjorken which allowed for a better description of the weak interaction and implied a mass formula that correctly reproduced the masses of the known mesons); in this case, ZEH has the advantage to can directly estimate these common/shared ratios:  $\phi_{\mathrm{g(u/cq)}}$  &  $\phi_{e(u/cq)}$  (shared by uq-cq) and  $\phi_{g(d/sq)}$  &  $\phi_{e(d/sq)}$  (shared by dqsq); for the uq-cq we have  $m_{uq} + m_{cq} = 2c^2/\phi_{g\,(\mathrm{u/cq})}$ , from which their common/shared  $\phi_{g(u/ ext{cq})}$  ratio can be reversely other  $\phi_{
m e(u/cq)}$  ratio can be also reversely estimated from both  $m_{cq}$ (or  $m_{uq}$ ) and  $\phi_{g(u/cq)}$  as  $\phi_{e(u/cq)} \cong 6.4 \times 10^{25} F^{-1}$ , with assigned  $k_{e(\text{u/cq})} = \phi_{e(\text{u/cq})} r_{\text{min}} \cong 10^{-20} k_e$ ; for dq-sq we have

estimated as  $\phi_{g(u/cq)} = 2c^2 / (m_{uq} + m_{cq}) \cong 7.8 \times 10^{43} u$ : the  $m_d + m_s = 2c^2 / \phi_{\sigma(d/s_0)}$ , from which their common/shared  $\phi_{g(d/sq)}$  $\phi_{g(d/\text{sq})} = 2c^2 / (m_{dq} + m_{sq}) \cong 10^{45} u$ : the other  $\phi_{e(d/\text{sq})}$  ratio

 $\phi_{\text{e(d/sq)}} \cong 5.1 \times 10^{26} F^{-1}$  $\phi_{g(d/sq)}$ with assigned  $k_{e(d/sq)} = \phi_{e(d/sq)} r_{min} \cong 7.9 \times 10^{-20} k_{e}$ 

(3) Another possibility is that only the first two generations of quarks may be actually reciprocally conjugated in fermion-fermion (quark-quark) pairs like uq-cq and dq-sq; the 3<sup>rd</sup> generation of quarks may actually be conjugated with two unknown "quark bosons" (with fractional charge) called here "top-boson" (**Tb**) (with **(Bb)** (with emc  $\pm 1/3$ e and conjugating to the bottom-quark).

emc ±2/3e and conjugating to the top-quark) and "bottom-boson" (4) In the case of the muon (m) and tauon (t) (which are currently considered two distinct excited states of the electron) ZEH offers two possibilities of mass-conjugation: (a) the muon and the tauon may be conjugated with two predicted hypothetical bosons (which are analogously considered two distinct excited (superheavy) states of the W boson) called here the "W muonic boson" (Wm) and the "W tauonic boson" (Wt) respectively, which Wm and Wt are probably much heavier than the W boson and the Higgs boson, thus indirectly suggesting the existence of the 4<sup>th</sup> generation of quarks (which may produced by the decay of these super-heavy Wm and Wt); (b) the  $2^{nd}$  possibility is that the muon (m) and tauon (t) could be actually reciprocal conjugates (thus not necessarily conjugated with other two [previously predicted] bosons [heavier than the W boson]: Wm and Wt),  $m_m + m_t = 2c^2 / \phi_{g(m/t)}$ , from which their common/shared estimated  $\phi_{g(m/t)} = 2c^2 / (m_m + m_t) \cong 5.36 \times 10^{43} u$ , approximately 15-20 times larger than  $\phi_{g(Zb)} \left(\cong 10^{42} u \right)$  and  $\phi_{g(Hb)} (\cong 8 \times 10^{41} u)$ . The other  $\phi_{e(m/t)}$  ratio can be also reversely estimated from both  $m_t$  (or  $m_m$ ) and  $\phi_{g(\mathrm{m/t})}$  as  $\phi_{e(m/t)} \cong 1.2 \times 10^{27} F^{-1}$ assigned  $k_{e(m/t)} = \phi_{e(m/t)} r_{min} \cong 1.9 \times 10^{-19} k_e$ 

(5) Analogously to the case of the muon (m) and tauon (t) ZEH also offers two additional possibilities of mass-conjugation in the case of the three known generations of quarks: (a) the 1<sup>st</sup> generation quarks (uq & dq) may be actually conjugated with two distinct quark bosons with fractional charge (the here called "up-boson" [Ub] with emc  $\pm 2/3e$  [conjugated to uq] and the "down-boson" [**Db**] with emc  $\pm 1/3e$  [conjugated to dq]) and the other two quark generations (cq & tq [which are considered two distinct excited states of the same uq] plus sq & bq [which are considered two distinct excited states of the same dq]) may be actually reciprocal conjugates on horizontal so that  $m_{cq} + m_{tq} = 2c^2/\phi_{g(c/tq)}$  (and  $m_{sq} + m_{bq} = 2c^2 / \phi_{g(s/bq)}$  respectively), from which their can be also reversely estimated from both  $m_{dq}$  (or  $m_{sq}$ ) and common/shared  $\phi_{g(c/tq)}$  ratio (and  $\phi_{g(s/bq)}$  ratio respectively) reversely estimated

$$\phi_{g(c/tq)} = 2c^2 / \left(m_{cq} + m_{tq}\right) \cong 5.7 \times 10^{41} u \qquad \text{(and } \phi_{g(s/bq)} = 2c^2 / \left(m_{sq} + m_{bq}\right) \cong 2.3 \times 10^{43} u \qquad \text{respectively): the other } \phi_{e(c/tq)} \text{ ratio can be also reversely estimated from both } m_{tq} \qquad \text{(or } m_{cq} \text{) and } \phi_{g(c/tq)} \text{ as } \phi_{e(c/tq)} \cong 3.6 \times 10^{28} F^{-1} \qquad \text{with assigned } k_{e(c/tq)} = \phi_{e(c/tq)} r_{\min} \cong 5.5 \times 10^{-18} k_e \text{ ; the other } \phi_{e(s/bq)} \text{ ratio can be also reversely estimated from both } m_{bq} \text{ (or } m_{sq} \text{) and } \phi_{g(s/bq)} \text{ as } \phi_{e(s/bq)} \cong 1.05 \times 10^{28} F^{-1} \text{ with assigned } k_{e(s/bq)} = \phi_{e(s/bq)} r_{\min} \cong 1.6 \times 10^{-18} k_e \text{ .}$$

In a checkpoint conclusion, what distinguishes ZEH is actually the contrast between its simplicity and the richness/diversity of explanations, correlations and predictions it offers. The author of this paper resonates to the famous Dirac's vision on the importance of mathematical beauty in physical equations: "The research worker, in his efforts to express the fundamental laws of Nature in mathematical form, should strive mainly for mathematical beauty [...] It often happens that the requirements and beauty are the same, but where they clash the latter must take precedence."

#### **III. Discussion**

The energy/length scale-dependent electro-gravitational resistivity of vacuum R(E) (introduced in the 1st section of this paper) is a powerful concept which predicts the existence of the graviton (as a spin-2 boson with an assigned Planck-like gravitational constant  $h_g << h$  measuring its quantum angular momentum), retrodicts a minimum quantum angular momentum h for electromagnetic waves (thus the quantum nature of photons), predicts a maximum speed  $v_{\max} \left(= c = v_g\right)$  for any physical wave allowed in our universe and predicts both a variable  $G_q(E)(>> G)$  and  $\alpha(E)$  bringing General relativity and quantum field theory more closer to one another by offering a solution to the hierarchy problem in physics.

The zero-energy hypothesis (**ZEH**) proposed in this paper is another powerful concept which is essentially a *conservation* principle applied on zero-energy that mainly states a general quadratic equation having a pair of conjugate mass solutions for each set of coefficients, thus predicting a new type of mass "symmetry" called here "mass conjugation" between elementary particles which predicts the zero/non-zero rest masses of all known/unknown EPs to be conjugated in boson-fermion pairs; more specifically, ZEH proposes a general formula for all the rest masses of all elementary particles from Standard model, also indicating a possible bijective connection between the three types of neutrinos and the massless bosons (photon, gluon and the hypothetical

graviton), between the electron/positron and the W boson and predicting two distinct types of neutral massless fermions (modelled as conjugates of the Higgs boson and Z boson respectively) which are plausible candidates for dark energy and dark matter. ZEH also offers a new interpretation of Planck length as the approximate length threshold above which the rest masses of all known elementary particles have real number values (with mass units) instead of complex/imaginary number values (as predicted by the unique quadratic equation proposed by ZEH). ZEH also helps correcting R(E) as based on the currently known the leading log approximation (LLA) of  $\alpha(E) \Big[ = \alpha_0 / (1 - \alpha_0 f(E)) \Big]$  and predicts the behaviour of the electromagnetic field and gravitational field at Planck length/energy scales; ZEH also predicts the existence

# IV. Final conclusions

of a pre-Big Bang quasi-singularity with large but finite density.

The combination between the concept of *electrogravitational* resistivity of vacuum and the zero-energy hypothesis may help solving the hierarchy problem, the infinite-density singularity problem (of General relativity) and crystallizes new directions in theoretical physics beyond the Standard model, including the prediction of two massless fermions (that represent good candidates for dark energy and dark matter) and the existence of a pre-Big Bang quasi-singularity with large but finite density.

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